

# Trigonometry - ANSWERS

## T1 Exercises

1.  $20.075^\circ$

5.  $15.168^\circ$

9.  $65^\circ 0' 5''$

13.  $83^\circ 59'$

17.  $28^\circ 03' 03''$

21.  $45^\circ, 135^\circ$

25.  $180 - \theta^\circ$

3.  $274.304^\circ$

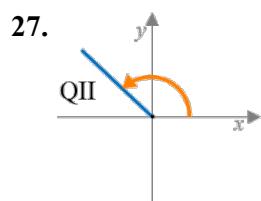
7.  $18^\circ 0' 45''$

11.  $175^\circ 23' 58''$

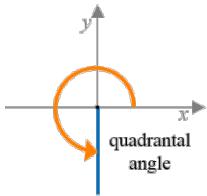
15.  $33^\circ 50'$

19.  $60^\circ, 150^\circ$

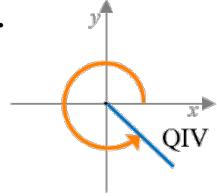
23.  $74^\circ 30', 164^\circ 30'$



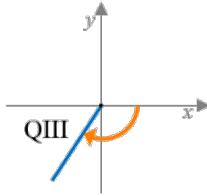
29.



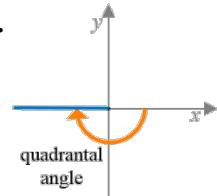
31.



33.



35.



37.  $15^\circ$

41.  $30^\circ + k \cdot 360^\circ$

45.  $\alpha^\circ + k \cdot 360^\circ$

39.  $135^\circ$

43.  $k \cdot 360^\circ$

47.  $7.5^\circ$

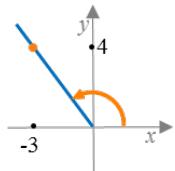
## T2 Exercises

1.  $\sin \theta = \frac{3}{5}$ ,  $\cos \theta = \frac{4}{5}$ ,  $\tan \theta = \frac{3}{4}$ ,  $\csc \theta = \frac{5}{3}$ ,  $\sec \theta = \frac{5}{4}$ ,  $\cot \theta = \frac{4}{3}$

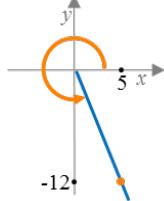
3.  $\sin \theta = \frac{\sqrt{3}}{2}$ ,  $\cos \theta = \frac{1}{2}$ ,  $\tan \theta = \sqrt{3}$ ,  $\csc \theta = \frac{2\sqrt{3}}{3}$ ,  $\sec \theta = 2$ ,  $\cot \theta = \frac{\sqrt{3}}{3}$

5.  $\sin \theta = \frac{n}{\sqrt{n^2+4}} = \frac{n\sqrt{n^2+4}}{n^2+4}$ ,  $\cos \theta = \frac{2}{\sqrt{n^2+4}} = \frac{2\sqrt{n^2+4}}{n^2+4}$ ,  $\tan \theta = \frac{n}{2}$ ,  $\csc \theta = \frac{\sqrt{n^2+4}}{n}$ ,  $\sec \theta = \frac{\sqrt{n^2+4}}{2}$ ,  $\cot \theta = \frac{2}{n}$

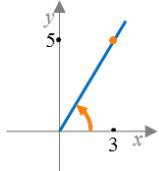
7.  $\sin \theta = \frac{4}{5}$ ,  $\cos \theta = -\frac{3}{5}$ ,  $\tan \theta = -\frac{4}{3}$



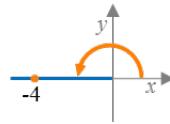
9.  $\sin \theta = -\frac{12}{13}$ ,  $\cos \theta = \frac{5}{13}$ ,  $\tan \theta = -\frac{12}{5}$



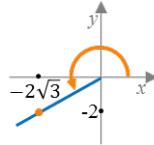
13.  $\sin \theta = \frac{5\sqrt{34}}{34}$ ,  $\cos \theta = \frac{3\sqrt{34}}{34}$ ,  $\tan \theta = \frac{5}{3}$



11.  $\sin \theta = 0$ ,  $\cos \theta = -1$ ,  $\tan \theta = 0$



15.  $\sin \theta = -\frac{1}{2}$ ,  $\cos \theta = -\frac{\sqrt{3}}{2}$ ,  $\tan \theta = \frac{\sqrt{3}}{3}$



17. sine, cosine, cosecant and secant are negative, tangent and cotangent are positive

19. negative

21. negative

23. positive

25. positive

27. negative

29. 1

31. -1

33. 0

35. undefined

37. 0

39.  $\cos \beta = -\frac{\sqrt{5}}{3}$

$\tan \beta = \frac{2\sqrt{5}}{5}$

### T3 Exercises

1. 0.6000      3. -0.9106  
 5.  $\frac{\sqrt{2}}{2}$       7.  $\frac{\sqrt{3}}{2}$   
 9.  $\frac{1}{2}$       11. 1  
 13.  $\cos 67.5^\circ$       15.  $82^\circ$   
 17.  $13^\circ$       19.  $6^\circ$   
 21. QIII and QIV      23. QII  
 25. QIV      27. negative  
 29. negative      31. positive  
 33. positive      35.  $\frac{\sqrt{3}}{2}$   
 37.  $\frac{1}{2}$       39.  $-\frac{\sqrt{3}}{2}$   
 41. 1      43.  $60^\circ, 300^\circ$   
 45.  $60^\circ, 120^\circ$       47.  $135^\circ, 225^\circ$   
 49.  $150^\circ, 330^\circ$       51.  $\sin \alpha = -\frac{4}{5}$   
                                    $\tan \alpha = -\frac{4}{3}$

### T4 Exercises

1.  $52.2^\circ$       3.  $68.4^\circ$       5.  $60^\circ$   
 7.  $\angle B = 54^\circ$ ,  $b \approx 16.5$ ,  $c \approx 20.4$       9.  $\angle A \approx 31.0^\circ$ ,  $\angle B \approx 59.0^\circ$ ,  $c \approx 17.5$   
 11.  $\angle A \approx 74.4^\circ$ ,  $\angle B \approx 15.6^\circ$ ,  $b \approx 2.6$       13.  $a = 2\sqrt{3}$ ,  $b = 6\sqrt{3}$ ,  $d = 4\sqrt{3}$ ,  $h = 6$   
 15.  $a = 5$ ,  $b = \frac{5}{2}$ ,  $h = \frac{5\sqrt{3}}{2}$ ,  $s = 5$       17.  $32\sqrt{3}$  cm  
 19.  $23^\circ$       21. 700 m  
 23. 317 m      25. 1101 km; direction of  $107^\circ$  (or S $73^\circ$ E)  
 27. 552 m; 447 m      29. 29.6 m      31. 237 m

## T5 Exercises

1.  $\angle P = 39^\circ$ ,  $p \approx 15.3$  cm,  $s \approx 22.8$  cm
5.  $\angle I \approx 19.8^\circ$ ,  $i \approx 8.8$  cm,  $\angle J \approx 122.2^\circ$
9.  $\angle A \approx 25.6^\circ$ ,  $a \approx 10.5$ ,  $\angle B \approx 9.4^\circ$
13.  $p \approx 19.8$  m,  $\angle R \approx 33.1^\circ$ ,  $\angle S \approx 129.9^\circ$
17.  $\angle A \approx 17^\circ$ ,  $\angle B \approx 103^\circ$ ,  $c \approx 8.9$
21. No, because the ratio of sines of angles is not the same as the ratios of those angles.  
For instance,  $\frac{\sin 90^\circ}{\sin 45^\circ} = \sqrt{2} \neq \frac{90^\circ}{45^\circ} = 2$ .
23. 128 m
27.  $\sim 6.4$  m
31.  $\sim 777$  km; direction:  $\sim 279^\circ 2'$
35.  $\sim 76$  m
39.  $\sim 69^\circ$
3.  $\angle A \approx 25.9^\circ$ ,  $\angle C \approx 18.1^\circ$ ,  $c \approx 19.3$  ft
7.  $b = 10$ ,  $\angle C = 120^\circ$ ,  $c \approx 17.3$
11.  $\angle X \approx 40.6^\circ$ ,  $y \approx 18.4$  m,  $\angle Z \approx 54.4^\circ$
15.  $\angle I \approx 48.5^\circ$ ,  $\angle J \approx 86.3^\circ$ ,  $\angle K \approx 45.2^\circ$
19.  $\angle A \approx 29.0^\circ$ ,  $\angle B \approx 46.6^\circ$ ,  $\angle C \approx 104.4^\circ$
25. 8.1 km; 11.0 km
29.  $\sim 351$  m from  $A$ ;  $\sim 295$  from  $B$
33.  $\sim 26^\circ$
37.  $\sim 1199$  m<sup>2</sup>
41.  $\sim 663.5$  m<sup>2</sup>