## Unit 2

## Percent

## Topic A: Introducing Percent

Percents are another form of fractions and are used in many everyday situations. Interest rates, credit card charges, taxes, pay deductions, increases and decreases are all calculated with percent. Percents are a convenient way to express part of the whole thing because the unwritten denominator is always 100 .

- the denominator of 100 is not written or said.
- a percent sign \% follows the number and is read as "percent".
- the whole thing is $100 \%$
- $100 \%=1$

Remember that cent is the Latin word meaning a hundred or a hundredth. And per is a Latin word meaning by or for each. So, percent means for each hundred.

## Reading and Writing Percents

## To write a percent

- write the number in the usual way
- place the percent sign after the numerals

$$
\begin{aligned}
& 50 \% \\
& 5 \frac{1}{2} \% \text { or } 5.5 \% \\
& \frac{3}{4} \% \text { or } 0.75 \%
\end{aligned}
$$

## To read a percent

- read the numbers in the usual way
- say "percent" after the number
$16 \%$ say "sixteen percent"
$4 \frac{1}{2} \%$ say "four and one-half percent"
$0.25 \%$ say "twenty-five hundredths percent" , "one-quarter percent" or "point two five percent".


## Exercise One

a) thirty-four percent

Write these percents using numerals and a percent sign. Note that the mixed numbers may be expressed with common fractions or decimals.
b) twelve percent
c) four-fifths percent
d) one hundred sixteen and three-tenths percent
e) thirteen percent
f) six and one-fifth percent
g) ninety-four and one-half percent $\qquad$
h) one-tenth percent
i) one hundred percent
j) one hundred fifty percent $\qquad$

Answers to Exercise One
b) $12 \%$
c) $0.8 \%$ or $\frac{4}{5} \%$
d) $116.3 \%$ or $116 \frac{3}{10} \%$
e) $13 \%$
f) $6.2 \%$ or $6 \frac{1}{5} \%$
g) $94.5 \%$ or $94 \frac{1}{2} \%$
h) $0.1 \%$ or $\frac{1}{10} \%$
i) $100 \%$
j) $150 \%$
a) $62 \%$
b) $371 / 2 \%$
c) $202 \%$
d) $3 / 4 \%$
e) $1 \frac{1}{4} \%$
f) $18.3 \%$
g) $14 \%$
h) $0.5 \%$
i) $1 / 2 \%$
j) $25 \%$
k) $100 \%$
sixty-two percent
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answers to Exercise Two

b) thirty-seven and one-half percent
c) two hundred two percent
d) three-quarters percent
f) eighteen and three-tenths percent
e) one and one-quarter percent
g) fourteen percent
h) five-tenths percent or one-half percent or zero point five percent j) twenty-five percent
i) one-half percent
k) one hundred percent

## Changing Decimals to Percents

Writing equivalent fractions is an important math skill.
Equivalent common fractions, decimals, and percents all represent the same amount.

$$
\begin{aligned}
& \frac{1}{2}=0.5=50 \% \\
& \frac{3}{10}=0.3=30 \%
\end{aligned}
$$

You need the skill of writing equivalent fractions for working with percents.

> To change any number to a percent, multiply the number by $100 \%$ and place a percent sign $\%$ after the product.

Remember this shortcut for multiplying by 100 ?
$4.27 \times 100=427$
$0.287 \times 100=28.7$
$53 \times 100=5300$

The shortcut is: When multiplying by 100 , move the decimal point two places to the right.

Example A: Change these numbers to a percent.

| 1 | $1 \times 100 \%$ | $=$ | $100 \%$ |
| :--- | :--- | :--- | :--- |
| 0.25 | $0.25 \times 100 \%$ | $=$ | $25 \%$ |
| 0.8 | $0.8 \times 100 \%$ | $=$ | $80 \%$ |
| 0.375 | $0.375 \times 100 \%$ | $=$ | $37.5 \%$ |

So...

To change a decimal to a percent, move the decimal point two places to the right and then write the percent sign after the number.

Examples: Change each decimal to a percent.

$$
\begin{aligned}
& 0.125=0.12 .5=12.5 \% \\
& 1.375=1.37 .5=137.5 \%
\end{aligned}
$$

If the decimal point moves to the end of the number it is not necessary to write the decimal point. Remember that zeros at the beginning of a number are also not necessary.

$$
\begin{aligned}
& 0.24=0.24 .=\npreceq 24 \%=24 \% \\
& 0.05=0.05 \cdot=\not \emptyset \not \boxed{5} \%=5 \%
\end{aligned}
$$

If the decimal is a tenth (one decimal place), it will be necessary to add a zero. If you are changing a whole number to a percent, add two zeros.

$$
\begin{aligned}
& 0.4=0.40 .=40 \% \\
& 1.7=1.70 .=170 \% \\
& 2=2.00 .=200 \%
\end{aligned}
$$

Exercise Three

|  | Decimal | $\times 100 \%$ <br> Move decimal 2 places <br> to right | $=$ |
| :--- | :--- | :---: | :--- |
| a) | 0.75 | 0.75. | $=$ |
| b) | 0.33 |  | $75 \%$ |
| c) | 0.1 |  |  |
| d) | 0.0025 |  |  |
| e) | 0.07 |  |  |
| f) | 0.9 |  |  |
| g) | 0.166 |  |  |
| h) | 0.43 |  |  |
| i) | 0.325 |  |  |
| j) | 0.088 |  |  |
| k) | 0.0625 |  |  |
| l) | 2.75 |  |  |
| m) | 1.36 |  |  |
| n) | 0.001 |  |  |
| o) | 0.68 |  |  |
| p) | 3 |  |  |
| q) | 0.688 |  |  |
| r) | 1.9 |  |  |

## Answers to Exercise Three

b) $33 \%$
c) $10 \%$
d) $0.25 \%$
e) $7 \%$
f) $90 \%$
g) $16.6 \%$
h) $43 \%$
i) $32.5 \%$
j) $8.8 \%$
k) $6.25 \%$

1) $275 \%$
m) $136 \%$
n) $0.1 \%$
r) $190 \%$

## Changing Percents to Decimals

Review Dividing by 100 :

$$
\begin{aligned}
& 47.39 \div 100=0.4739 \\
& 429 \div 100=4.29 \\
& 3.824 \div 100=0.03824
\end{aligned}
$$

To divide by 100, move the decimal point two places to the left.

Examples: Change each percent to a decimal or mixed number.

$$
\begin{array}{rrll}
58 \%=58 \div 100= & .58= & 0.58 \\
20 \%= & 20 \div 100= & .2= & 0.2 \\
6 \% & =6 \div 100= & .06= & 0.06 \\
110 \% & =110 \div 100 & =1.10 &
\end{array}
$$

So...

To change a percent to a decimal, divide by 100 (move the decimal point two places to the left) and remove the percent sign.

Examples: Change each percent to a decimal .

$$
\begin{aligned}
& 75 \%=75.0 \% \\
& 12 \%=0.75 \\
& 37.5 \%=37.5 \% \\
&=12.0 \%=0.12 \\
& 125 \%=125.0 \% \\
&=1.25 \\
& 5 \%=5.0 \%
\end{aligned}=0.050=0.046
$$

## Some notes to remember:

- If there is no decimal point in the percent, place the decimal point after the last numeral and then divide by 100 .

$$
24 \%=24 . \%=0.24
$$

- It may be necessary to prefix zeros. (This means adding zeros in front of the number, if needed)

$$
6 \%=6 . \%=0.06
$$

- A zero at the right of a decimal is not needed and may be left off.

$$
40 \%=40 . \%=.40=0.4
$$

Change each percent to its decimal equivalent.

|  | Percent | $\begin{gathered} \div 100 \\ \text { Move decimal } 2 \text { places } \\ \text { to left } \\ \hline \end{gathered}$ | $=$ Decimal |
| :---: | :---: | :---: | :---: |
| a) | 23\% | . 23. | $=0.23$ |
| b) | 1\% |  |  |
| c) | 9.2\% |  |  |
| d) | 112\% |  |  |
| e) | 10.3\% |  |  |
| f) | 36\% |  |  |
| g) | 75\% |  |  |
| h) | 100\% |  |  |
| i) | 8.25\% |  |  |
| j) | 9\% |  |  |
| k) | 14\% |  |  |
| 1) | 5\% |  |  |
| m) | 4.4\% |  |  |
| n) | 147\% |  |  |
| o) | 11.5\% |  |  |
| p) | 18\% |  |  |
| q) | 4\% |  |  |
| r) | 200\% |  |  |

## Answers to Exercise Four

b) 0.01
c) 0.092
d) 1.12
e) 0.103
f) 0.36
g) 0.75
h) 1.00
i) 0.0825
ј) 0.09
k) 0.14

1) 0.05
m) 0.044
n) 1.47
o) 0.115
p) 0.18
q) 0.04
r) 2.00

To change a percent containing a common fraction to a decimal, do this:

- Change the common fraction in the percent to a decimal in the percent.
- Divide by 100 (move the decimal 2 places to the left).


## Examples:

$$
\begin{array}{lll}
3 \frac{1}{2} \%=3.5 \% & 3.5 \% \div 100=.035=0.035 \\
37 \frac{1}{2} \%=37.5 \% & 37.5 \% \div 100=.375=0.375 \\
\frac{1}{4} \% & =0.25 \% & 0.25 \% \div 100=0.0025 \\
17 \frac{1}{3} \%=17.3 \% & 17 . \overline{3}^{3} \% \div 100=0.17 \overline{3}
\end{array}
$$

a) $8 \frac{4}{5} \%=$
$8.8 \%=0.088$
b) $4 \frac{1}{2} \%=$
c) $56 \frac{3}{4} \%=$
d) $1 \frac{3}{5} \%=$
e) $112 \frac{1}{2} \%=$ $\qquad$ f) $2 \frac{3}{8} \%=$ $\qquad$
g) $5 \frac{1}{4} \%=$ $\qquad$ h) $1 \frac{1}{2} \%=$ $\qquad$
i) $2 \frac{1}{8} \%=$ $\qquad$ j) $77 \frac{1}{2} \%=$ $\qquad$

## Answers to Exercise Five

b) 0.045
c) 0.5675
d) 0.016
e) 1.125
f) 0.02375
j) 0.775

## Changing Common Fractions to Percents

To change any number to a percent, multiply the number by $100 \%$ and place the percent sign $\%$ after the product.

There are two methods you can use to change a common fraction to a percent.

## Method One:

To change a common fraction to an equivalent percent, multiply the common fraction by $\mathbf{1 0 0 \%}$.

## Examples:

$\frac{3}{4}=\_\% \quad \frac{3}{4} \times 100 \%=\frac{3}{A_{1}} \times \frac{\not \partial \varnothing \varnothing^{25}}{1}=75 \%$
$\frac{5}{8}=\ldots \% \quad \frac{5}{8} \times 100 \%=\frac{5}{夕_{2}} \times \frac{\not \partial \not \varnothing^{25}}{1}=\frac{125}{2} \%=62.5 \%$
$\frac{7}{10}=\_\%$
$\frac{7}{10} \times 100 \%=\frac{7}{\not \varnothing_{1}} \times \frac{\not \varnothing \varnothing \varnothing^{10}}{1}=70 \%$
$1 \frac{1}{5}=\ldots \%$
$1 \frac{1}{5} \times 100 \%=\frac{6}{\not \Phi_{1}} \times \frac{\not \partial \emptyset \varnothing^{20}}{1}=120 \%$

Multiply by $100 \%$ to change each common fraction to an equivalent percent.
a) $\frac{4}{5} \quad \frac{4}{5} \times 100 \%=80 \%$
b) $\frac{1}{5}$ $\qquad$
c) $\frac{9}{10}$
d) $1 \frac{1}{2}$ $\qquad$
e) $\frac{7}{10}$ $\qquad$
f) $3 \frac{3}{4}$ $\qquad$
g) $\quad 15 \frac{1}{4}$ $\qquad$ h) $\frac{3}{20}$ $\qquad$
i) $\frac{17}{25}$ $\qquad$
j) $\frac{1}{3}$ $\qquad$
k) $\frac{7}{50}$ $\qquad$ 1) $\frac{1}{2}$ $\qquad$
m) $\frac{16}{20}$ $\qquad$ n) $\frac{1}{4}$ $\qquad$

## Answers to Exercise Six

b) $20 \%$
c) $90 \%$
d) $150 \%$
e) $70 \%$
f) $375 \%$
g) $1525 \%$
h) $15 \%$
i) $68 \%$
j) $33 \frac{1}{3} \%$
k) $14 \%$

1) $50 \%$
m) $80 \%$
n) $25 \%$

## Method Two:

To change a common fraction to an equivalent percent, first write the common fraction as a decimal. Then multiply the decimal by $100 \%$ (move the decimal point two places to the right).
$\frac{3}{8}=\ldots \%$
0.375
$8 \longdiv { 3 . 0 0 0 }$
$24 \downarrow \downarrow$
$60 \downarrow$
$\frac{56}{46} \downarrow$

$$
\frac{3}{8}=0.375 \quad 0.37 .5=37.5 \%
$$

$$
\frac{1}{3}=\ldots \%
$$

$$
\frac{0.33 \overline{3}}{3 \longdiv { 1 . 0 0 0 }}
$$

$$
0.33 \cdot \overline{3}=33 . \overline{3} \%
$$

$$
\text { also written as } 33 \frac{1}{3} \%
$$

$$
\frac{11}{12}=\ldots \% \quad \begin{array}{r}
12 \begin{array}{r}
0.9166 \\
\frac{11.000}{10} \\
20 \downarrow \\
\frac{12}{80} \\
\frac{72}{8}
\end{array}
\end{array} \quad 0.91 \cdot \overline{6}=91 . \overline{6} \%
$$

Exercise Seven
Change each common fraction to an equivalent percent by first writing a decimal.
a) $\frac{1}{12}=0.08 \overline{3} \quad 0.08 \overline{3} \times 100 \%=8 . \overline{3} \%$
b) $\frac{1}{8}$
c) $\frac{5}{8}$
d) $\frac{7}{8}$
f) $\frac{2}{3}$
e) $12 \frac{1}{5}$ $\qquad$ f) 3
g) $7 \frac{1}{3}$
h) $\frac{5}{16}$
) $\frac{5}{6}$
$\qquad$
j) $\frac{4}{9}$
k) $\frac{1}{6}$

1) $\frac{40}{45}$

## Answers to Exercise Seven

b) $12.5 \%$
c) $62.5 \%$
d) $87.5 \%$
e) $1220 \%$
f) $66.6 \%$
g) $733.3 \%$
h) $31.25 \%$
i) $83.3 \%$
j) $44.4 \%$
k) $16.6 \%$
l) $88.8 \%$

The method you use to change a common fraction to a percent will depend on the numbers you are working with. Choose whichever method seems easier for the situation. You will also memorize many equivalencies as you work with them. But you should definitely
memorize $\frac{1}{3}=33 \frac{1}{3} \%$ and $\frac{2}{3}=66 \frac{2}{3} \%$.

## Changing Percents to Common Fractions

You know that percents are a form of fraction with an unwritten denominator of $100 . \mathrm{A} \%$ sign is used.

To change any percent to a decimal, common fraction, or mixed number, divide by 100 and remove the percent sign.

To change a percent to a common fraction:

- write the numerals in the percent as the numerator.
- write 100 as the denominator. (Remember that the line in a fraction can be a divided by sign, so $58 \%=\frac{58}{100}$ is the same as $58 \div 100$.)
- remove the $\%$ sign.
- simplify the fraction: $\frac{58}{100}=\frac{29}{50}$

Examples: Write each percent as a common fraction.

$$
\begin{aligned}
& 38 \%=\frac{38}{100}\left(\frac{\div 2}{\div 2}\right)=\frac{19}{50} \\
& 25 \%=\frac{25}{100}\left(\frac{\div 25}{\div 25}\right)=\frac{1}{4} \\
& 3 \%=\frac{3}{100}
\end{aligned}
$$

Note that percents greater than or equal to 100 become improper fractions which will be rewritten as mixed numbers.

$$
\begin{array}{lr}
110 \%=\frac{110}{100}=1 \frac{10}{100}=1 \frac{1}{10} & 1 0 0 \longdiv { \frac { 1 } { 1 1 0 } } \begin{array} { l } 
{ \frac { 1 0 0 } { 1 0 } } \\
{ 1 2 0 \% = \frac { 1 2 0 } { 1 0 0 } = 1 \frac { 2 0 } { 1 0 0 } = 1 \frac { 1 } { 5 } }
\end{array} \begin{array} { r } 
{ \frac { 1 } { \frac { 1 0 0 } { 2 0 } } }
\end{array}
\end{array}
$$

$\underset{\sim}{\boldsymbol{L}}$ Remember $100 \%$ is the whole thing. $\mathbf{1 0 0 \%}=\mathbf{1}$

Exercise Eight

Change each percent to a common fraction. Simplify to lowest terms.
a) $31 \%=$
b) $11 \%=$ $\qquad$
c) $2 \%=$
d) $78 \%=$ $\qquad$
e) $20 \%=$ $\qquad$
f) $50 \%=$ $\qquad$
g) $75 \%=$ $\qquad$
h) $60 \%=$ $\qquad$
i) $8 \%=$ $\qquad$
j) $95 \%=$ $\qquad$
k) $16 \%=$

1) $3 \%=$
m) $74 \%=$
n) $100 \%=$ $\qquad$
o) $135 \%=$ $\qquad$
p) $750 \%=$ $\qquad$
q) $400 \%=$ $\qquad$
r) $320 \%=\square$
s) $180 \%=$ $\qquad$
t) $282 \%=$ $\qquad$

## Answers to Exercise Eight

a) $\frac{31}{100}$
b) $\frac{11}{100}$
c) $\frac{1}{50}$
d) $\frac{39}{50}$
e) $\frac{1}{5}$
f) $\frac{1}{2}$
g) $\frac{3}{4}$
h) $\frac{3}{5}$
i) $\frac{2}{25}$
j) $\frac{19}{20}$
k) $\frac{4}{25}$

1) $\frac{3}{100}$
m) $\frac{37}{50}$
n) 1
o) $1 \frac{7}{20}$
p) $7 \frac{1}{2}$
q) 4
r) $3 \frac{1}{5}$
s) $1 \frac{4}{5}$
t) $2 \frac{41}{50}$

## Percents Less than 1\%

Sometimes a percent smaller than $\mathbf{1 \%}$ is used. For example, you will hear amounts such as $\frac{1}{4} \%$ or $\frac{1}{8} \%$ or $\frac{1}{2} \%$ on the news about the Bank of Canada rate and the rise and fall of inflation. These are small amounts. Sometimes the expression " $\frac{1}{2}$ of a percentage point" is used instead of " $\frac{1}{2} \%$ ".
What is $\frac{1}{4} \%$ ?

$$
\begin{aligned}
& \frac{1}{4} \% \text { is } \frac{1}{4} \text { of } 1 \% \\
& 1 \%=\frac{1}{100} \text { so } \frac{1}{4} \text { of } 1 \%=\frac{1}{4} \times \frac{1}{100}=\frac{1}{400} \\
& \frac{1}{4} \%=0.25 \%=0.0025
\end{aligned}
$$

What is $\frac{1}{2} \%$ ?

$$
\frac{1}{2} \%=\frac{1}{2} \text { of } 1 \%=\frac{1}{2} \times \frac{1}{100}=\frac{1}{200}
$$

$$
\frac{1}{2} \%=0.5 \%=0.005
$$

To work with percents less than $1 \%$, change the percent to a decimal by dividing by 100 (move decimal point two places to the left).

$$
0.2 \%=0.002 \quad 0.75 \%=0.0075
$$

## If the percent is expressed as a common fraction, do this:

- Write the common fraction percent as a decimal percent.
- Divide by 100 (move decimal point two places left).

$$
\begin{array}{lllll}
1 / 2 \% & =0.5 \% & =0.005 & 1 / 4 \% & =0.25 \% \\
1 / 8 \% & =0.125 \% & =0.00125 & &
\end{array}
$$

Exercise Nine
Change each percent to an equivalent decimal.
a) $\frac{1}{2} \%=$ $\qquad$ b) $0.6 \%=$ $\qquad$
c) $\frac{3}{10} \%$ $\qquad$ d) $\frac{3}{5} \% \quad=$
e) $0.75 \%=$ $\qquad$
f) $\frac{3}{4} \% \quad=\square$
g) $0.5 \%=$
h) $\frac{1}{4} \% \quad=$
i) $0.125 \%=$ $\qquad$
j) $\frac{1}{3} \%$
$=$ $\qquad$
k) $\frac{1}{8} \%=$ $\qquad$

1) $\frac{5}{8} \%$ $\qquad$
m) $\frac{1}{16} \%=$ $\qquad$
n) $\frac{2}{5} \%=$ $\qquad$

## Answers to Exercise Nine

a) 0.005
b) 0.006
c) 0.003
d) 0.006
e) 0.0075
f) 0.0075
g) 0.005
h) 0.0025
i) 0.00125
j) $0.00 \overline{3}$
m) 0.000625
n) 0.004
$16 \frac{2}{3} \%, 33 \frac{1}{3} \%, 66 \frac{2}{3} \%, 83 \frac{1}{3} \% \ldots$
These percents will become repeating decimals. For example

$$
\begin{aligned}
& 33 \frac{1}{3} \%=33 . \overline{3} \%=0.33 \overline{3} \\
& 66^{\frac{2}{3}} \%=66 . \overline{6} \%=0.66 \overline{6}
\end{aligned}
$$

It is usually more convenient to use the common fraction equivalent of these percents. Memorize them, or make a note on a special paper and post it near your work space.

$$
\begin{aligned}
& 33 \frac{1}{3} \%=33^{\frac{1}{3}} \div 100=\frac{100}{3} \times \frac{1}{100}=\frac{1}{3} \\
& 66^{\frac{2}{3}} \%=66^{\frac{2}{3}} \div 100=\frac{200}{3} \times \frac{1}{100}=\frac{2}{3}
\end{aligned}
$$

$$
\begin{aligned}
& 16 \frac{2}{3} \%=\frac{1}{6} \\
& 33 \frac{1}{3} \%=\frac{1}{3} \\
& 66 \frac{2}{3} \%=\frac{2}{3} \\
& 83 \frac{1}{3} \%=\frac{5}{6}
\end{aligned}
$$

## Review of Equivalent Common Fractions, Decimals, and Percents

Complete this chart. These are equivalents that you will often use, so use this chart for reference.
Memorize as many equivalents as you can. You may wish to put other equivalents on the chart.

| Common Fraction | Decimal | Percent |
| :--- | :--- | :--- |
|  | 0.5 |  |
|  |  | $75 \%$ |
| $\frac{1}{8}$ |  |  |
|  | 0.375 | $62.5 \%$ |
| $\frac{7}{8}$ |  |  |
|  |  |  |
| $\frac{3}{2}=\frac{3}{3}=\frac{4}{4}=\frac{5}{5}=1$ | 0.2 | $40 \%$ |
|  | 0.8 |  |
|  |  |  |
|  |  |  |
|  |  |  |


| $\frac{1}{6}$ | $0.3 \overline{3}$ |  |
| :--- | :--- | :--- |
|  |  |  |
|  | $\frac{5}{6}$ | 0.1 |
|  |  | $6 . \overline{6} \%$ |
|  |  |  |
| $\frac{7}{8}$ | 0.9 | $30 \%$ |
|  | 1 |  |
|  |  |  |

Answers to Review of Equivalent Common Fractions, Decimals, and Percents

| Common Fraction | Decimal | Percent |
| :---: | :---: | :---: |
| $\frac{1}{4}$ | 0.25 | 25\% |
| $\frac{1}{2}$ | 0.5 | 50\% |
| $\frac{3}{4}$ | 0.75 | 75\% |
| $\frac{1}{8}$ | 0.125 | 12.5\% |
| $\frac{3}{8}$ | 0.375 | 37.5\% |
| $\frac{5}{8}$ | 0.625 | 62.5\% |
| $\frac{7}{8}$ | 0.875 | 87.5\% |
| $\frac{1}{5}$ | 0.2 | 20\% |
| $\frac{2}{5}$ | 0.4 | 40\% |
| $\frac{3}{5}$ | 0.6 | 60\% |
| $\frac{4}{5}$ | 0.8 | 80\% |
| $\frac{2}{2}=\frac{3}{3}=\frac{4}{4}=\frac{5}{5}=1$ | 1 | 100\% |
| $\frac{1}{6}$ | $0.1 \overline{6}$ | 16. $\overline{6}$ \% |
| $\frac{1}{3}$ | $0.3 \overline{3}$ | $33 . \overline{3} \%$ or $33 \frac{1}{3} \%$ |
| $\frac{2}{3}$ | $0.6 \overline{6}$ | $66 . \overline{6} \%$ or $66{ }^{\frac{2}{3}} \%$ |
| $\frac{5}{6}$ | $0.8 \overline{3}$ | $83 . \overline{3} \%$ |
| $\frac{1}{10}$ | 0.1 | 10\% |
| $\frac{3}{10}$ | 0.3 | 30\% |
| $\frac{7}{8}$ | 0.875 | 87.5\% |
| $\frac{9}{10}$ | 0.9 | 90\% |
| e.g. $\frac{9}{9}$ | 1 | 100\% |

## A. Write these percents in numeral form.

a) sixty-two and one-half percent $\qquad$
b) eight percent $\qquad$
c) one hundred six and one-fifth percent
B. Write these percents in words.

3 marks
a) $72 \%$ $\qquad$
b) $120 \frac{1}{4} \%$ $\qquad$
c) $\frac{3}{4} \%$ $\qquad$
C. Change the percents to decimal fractions.

10 marks
a) $32 \%$
b) $10 \%$
c) $18.5 \%$
d) $125 \%$ $\qquad$
e) $1 \%$ $\qquad$ f) $0.25 \%$ $\qquad$
g) $\quad 44 \frac{1}{2} \%$ $\qquad$ h) $\frac{3}{4} \%$ $\qquad$
i) $\frac{4}{5} \%$ $\qquad$ j) $\frac{2}{3} \%$ $\qquad$
D. Change these percents to common fractions in lowest terms.

6 marks
a) $16 \%$
b) $20 \%$ $\qquad$
c) $106 \%$
d) $100 \%$ $\qquad$
e) $75 \%$
f) $5 \%$ $\qquad$
E. Change these common fractions to equivalent percents.

4 marks
a) $\frac{4}{5}$
b) $\frac{1}{4}$
c) $\frac{3}{8}$ $\qquad$ d) $\frac{11}{12}$

## Answers to Topic A Self-Test

## Part A

a) $62.5 \%$ or $62 \frac{1}{2} \%$
b) $8 \%$
c) $106.2 \%$ or $106 \frac{1}{5} \%$

## Part B

a) seventy-two percent
b) one hundred twenty and one-quarter percent
c) three-quarters percent

Part C
a) 0.32
b) 0.10
c) 0.185
d) 1.25
e) 0.01
f) 0.0025
g) 0.445
h) 0.0075
i) 0.008
j) $0.00 \overline{6}$

## Part D

a) $\frac{4}{25}$
b) $\frac{1}{5}$
c) $1 \frac{3}{50}$
d) 1
e) $\frac{3}{4}$
f) $\frac{1}{20}$

Part E
a) $80 \%$
b) $25 \%$
c) $37.5 \%$
d) $91 . \overline{6} \%$

## Unit 2 Review

1. Change these decimals to percents.
a) 0.75
b) 0.34
c) 0.156 $\qquad$ d) 0.03
e) 0.0035 $\qquad$ f) 0.625
h) 0.67
g) 0.048 $\qquad$
j) 2.37
2. Change each percent to a decimal.
a) $59 \%$
b) $42 \%$
c) $39.5 \%$
d) $152 \%$
e) $4.3 \%$ $\qquad$ f) $1 \%$
$\qquad$
g) $3 \frac{1}{2} \%$
h) $5 \frac{3}{4} \%$
i) $32 \frac{1}{3} \%$
j) $4 \frac{1}{4}$
k) $1 \frac{4}{5} \%$
1) $4 \frac{3}{5} \%$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
3. Change each fraction to an equivalent percent.
a) $\frac{6}{10}$
$\longrightarrow$
b) $1 \frac{3}{4}$
c) $\frac{1}{5}$
$\longrightarrow$
d) $4 \frac{3}{20}$
e) $\frac{5}{19}$ $\qquad$ f) $\frac{9}{20}$
g) $1 \frac{1}{4}$ $\qquad$ h) $2 \frac{1}{3}$
i) $\frac{7}{50}$ $\qquad$ j) $3 \frac{17}{25}$
$\qquad$
4. Change each percent to a common fraction. Simplify your answer.
a) $16 \%$ $\qquad$ b) $25 \%$
c) $110 \%$ $\qquad$ d) $95 \%$
e) $650 \%$ $\qquad$ f) $284 \%$ $\qquad$
g) $\frac{1}{4} \%$
$\longrightarrow$
h) $\frac{1}{2} \%$
i) $\frac{1}{8} \%$
$\longrightarrow$
j) $\frac{3}{5} \%$
k) $0.125 \%$ $\qquad$ 1) $\frac{1}{16} \%$ $\qquad$
m) $\frac{5}{8} \%$ $\qquad$ n) $0.7 \%$
o) $\frac{3}{4} \%$ $\qquad$ p) $0.25 \%$
5. Change each percent to a common fraction. These few should be memorized.
a) $33 \frac{1}{3} \%$
b) $66 \frac{2}{3} \%$
c) $16 \frac{2}{3} \%$
d) $83 \frac{1}{3} \%$

## Answers to Review

1. 

a) $75 \%$
b) $34 \%$
c) $15.6 \%$
d) $3 \%$
e) $0.35 \%$
f) $62.5 \%$
g) $4.8 \%$
h) $67 \%$
i) $345 \%$
2.
a) 0.59
b) 0.42
c) 0.395
d) 1.52
e) $0.04 \underline{3}$
f) 0.01
g) 0.035
h) 0.0575
i) 0.323
j) 0.0425
k) 0.018
l) 0.046
3.
a) $60 \%$
b) $175 \%$
c) $20 \%$
d) $415 \%$
e) $26.3 \%$
f) $45 \%$
g) $125 \%$
h) $233 . \overline{3} \%$
i) $14 \%$
j) $368 \%$
4.
a) $\frac{4}{25}$
b) $\frac{1}{4}$
c) $1 \frac{1}{10}$
d) $\frac{19}{20}$
e) $6 \frac{1}{2}$
f) $2 \frac{21}{25}$
g) $\frac{1}{400}$
h) $\frac{1}{200}$
i) $\frac{1}{800}$
j) $\frac{3}{500}$
k) $\frac{0.125}{100}$ or $\frac{1}{800}$

1) $\frac{1}{1600}$
m) $\frac{1}{160}$
n) $\frac{0.7}{100}$ or $\frac{7}{1000}$
o) $\frac{3}{400}$
p) $\frac{0.25}{100}$ or $\frac{1}{400}$
5. 

a) $\frac{1}{3}$
b) $\frac{2}{3}$
c) $\frac{1}{6}$
d) $\frac{5}{6}$

## TEST TIME!

## Ask your instructor for the Practice Test for this unit. <br> Once you've done the practice test, you need to do the unit 2 test.

Again, ask your instructor for this.

## Good luck!

